

## COMPARISON OF MECHANICAL AND ELECTRICAL PROPERTIES OF PIEZOELECTRIC COMPOSITES PZT/ZnO AND PZT/Al<sub>2</sub>O<sub>3</sub> FABRICATED BY POWDER METALLURGY

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**Abstract:** Lead zirconate titanate (PZT) as a piezoelectric ceramic has been used widely in the fields of electronics, biomedical engineering, mechatronics and thermoelectric. Although, the electrical properties of PZT ceramics is a major considerable, but the mechanical properties such as fracture strength and toughness should be improved for many applications. In this study, lead monoxide, zirconium dioxide and titanium dioxide were used to synthesize PZT compound with chemical formula  $Pb(Zr_{0.52}Ti_{0.48})O_3$  by calcination heat treatment. Planetary mill with zirconia balls were used for homogenization of materials. Two-stage calcination was performed at temperatures of 600°C and 850°C for holding time of 2h. In order to improve the mechanical properties of PZT, various amount of ZnO and/or Al<sub>2</sub>O<sub>3</sub> particles were added to calcined materials and so PZT/ZnO, PZT/Al<sub>2</sub>O<sub>3</sub> and PZT/ZnO+Al<sub>2</sub>O<sub>3</sub> composites were fabricated. Composites samples were sintered at 1100°C for 2 h in the normal atmosphere. Microstructural component and phase composition were analyzed by XRD and SEM. The density, fracture strength, toughness and hardness were measured by Archimedes method, three-point bending, direct measurement length crack and Vickers method, respectively. Dielectric and piezoelectric properties of the samples were also measured by LCR meter and d33meter tester, respectively. The results showed that by addition of ZnO and Al<sub>2</sub>O<sub>3</sub> to composite materials, the relative density of PZT based composites was increased in conjunction with a significant improvement of mechanical properties such as flexural strength, toughness and hardness. Moreover, the dielectric and piezoelectric properties of PZT such as dielectric constant, piezoelectric coefficient and coupling factor were decreased while the loss tangent was also increased.

**Keywords:** Al<sub>2</sub>O<sub>3</sub>+ZnO/PZT composites, powder metallurgy, mechanical properties, phase composition, microstructure.

### 1. INTRODUCTION

Lead zirconate titanate ceramics (PZT) due to their superior piezoelectric and ferroelectric properties have been used in numerous applications such as electronics, biomedical engineering, thermoelectric, mechatronics, ultrasonic generators, high frequency vibrators [1], activator [2], actuators sensors [3], capacitors aggravating, micro-electromechanical systems (MEMS) [4] and energy converters [5]. For compositions close to the morphotropic boundary phase (MBP) where the proportion of PbZrO<sub>3</sub>:PbTiO<sub>3</sub> is approximately 1:1, piezoelectric and dielectric properties have been significantly improved [6]. Although the electrical properties of PZT ceramics are good, but the mechanical properties such as fracture strength [7] and toughness are relatively poor for many

applications [8]. To increase the mechanical properties while maintaining the electrical properties of PZT ceramics, different PZT based composites with second phase as a reinforcing phase such as ZnO [9], Ag [10], Pt [11], MgO [12], ZrO<sub>2</sub> [12] and cement [13] have been developed. For the composites of PZT/Ag and PZT/Pt, the improvement of mechanical properties is much more significant key properties, while the reduction of electrical properties is not much considerable. However, the use of these elements is related to the higher cost and weight of the composites. In this work, the effect of ZnO and Al<sub>2</sub>O<sub>3</sub> as a secondary phase on sinterability, microstructural features, mechanical and electrical properties of PZT have been studied.

## 2. MATERIALS AND EXPERIMENTAL METHODS

Monolithic ceramic of PZT and PZT/Al<sub>2</sub>O<sub>3</sub> composites were prepared by a simple solid-state mixed oxide method. The starting powders of PbO (99.9%), ZrO<sub>2</sub> (99%) and TiO<sub>2</sub> (99%) were mixed in isopropanol using zirconia balls as a grinding media. Three oxides were mixed with ratios presented in Table 1 in order to obtain a compound with formulation of Pb(Zr<sub>0.52</sub>Ti<sub>0.48</sub>)O<sub>3</sub>.

The obtained slurry was dried for 4 hours at 100 °C. To evaluate the optimum temperature for heat treatment of calcination, differential thermal analysis (DTA) and thermal gravity (TG) tests are used in the condition of 1200 °C, argon atmosphere and the heating rate of 10 °C/min on powder mixture of PbO, TiO<sub>2</sub> and ZrO<sub>2</sub> (BAHR-Model STA 504). The homogenized powder was calcined at 600 °C/2h and 850 °C/2h with a heating rate of 1°C/min. The calcined PZT powders were mixed with ZnO or Al<sub>2</sub>O<sub>3</sub> and 2%wt PVA as a binder and ball milled in isopropanol for 24 h.

The slurry was then dried and sieved to a fine powder. The mixed powders were uniaxially pressed into pellets at a pressure of 200 MPa. The pellets were sintered in an alumina crucible at 1200 °C for 2h with a heating rate of 10 °C/min. A protecting layer of PbZrO<sub>3</sub> powder was applied to minimize PbO evaporation during sintering. However, an additional amount of approximately 0.2% lead oxide in primary mixture was considered. Density, linear shrinkage and phase composition were determined by Archimedes method, comparison dimensions of the sample before and after sintering and X-ray diffraction

(XRD), respectively. In order to microscopic observations by scanning electron microscopy (SEM), the sintered samples were polished and were etched in a chemical solution of 95% water and 5% mixture of 95%HCl and 5%HF solution. Fracture strength was carried out by three-point bending method (0.5 mm/min, 4mm × 4mm × 40mm). Fracture toughness was calculated by using direct measurements of the length of crack induced by Vickers indenter [14]:

$$K_{IC} = 0.018 \left( \frac{E}{H_V} \right)^{0.4} H_V a^{0.5} \left( \frac{l}{a} \right)^{-0.5} (MPa\sqrt{m}) \quad (1)$$

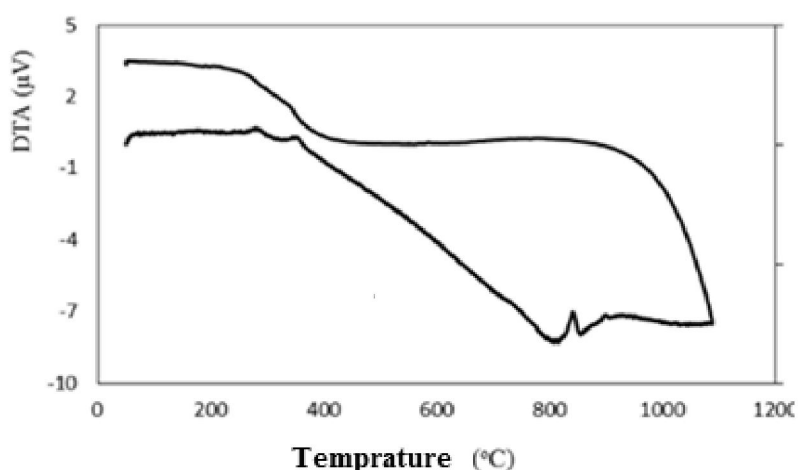
Where E is Young's modulus, H<sub>v</sub> is Vickers hardness, a is the half length of indentation, and L is the length of crack. The Young's modulus E<sub>com</sub> was obtained by using the mixture law:

$$E_{com} = E_{PZT}(1-x\%) + E_f x\%, \quad (2)$$

E<sub>PZT</sub> = 80 GPa, E<sub>f</sub> is modulus of reinforcing phase, and x was the volume fraction of reinforcing phase. At least three specimens were used for each measurement of density, hardness, fracture strength and toughness. For electrical measurement, both sides of the sintered pellets were polished, painted with silver paste and fired at 800 °C for 10 min. Prior to measurement of the piezoelectric constant by d33 meter tester, poling treatment was carried out in silicon oil at 20 °C for 20 min with an electric field of 3–4 kV/mm.

**Table 1.** The percentage by weight and volume fraction of raw materials for the composition of Pb(Zr<sub>0.52</sub>Ti<sub>0.48</sub>)O<sub>3</sub>

| Type of oxides   | Molecular mass (gr/mole) | Weight percent (%) | Volume percent (%) |
|------------------|--------------------------|--------------------|--------------------|
| PbO              | 223.2                    | 68.55              | 53.52              |
| TiO <sub>2</sub> | 79.866                   | 11.77              | 20.7               |
| ZrO <sub>2</sub> | 123.218                  | 19.69              | 25.78              |



a



b

**Fig. 1.** The variation of a: DTA b: TG curves obtained from the mixture of PbO, TiO<sub>2</sub> and ZrO<sub>2</sub> powders ball-milled for 1h.

### 3. RESULTS AND DISCUSSION

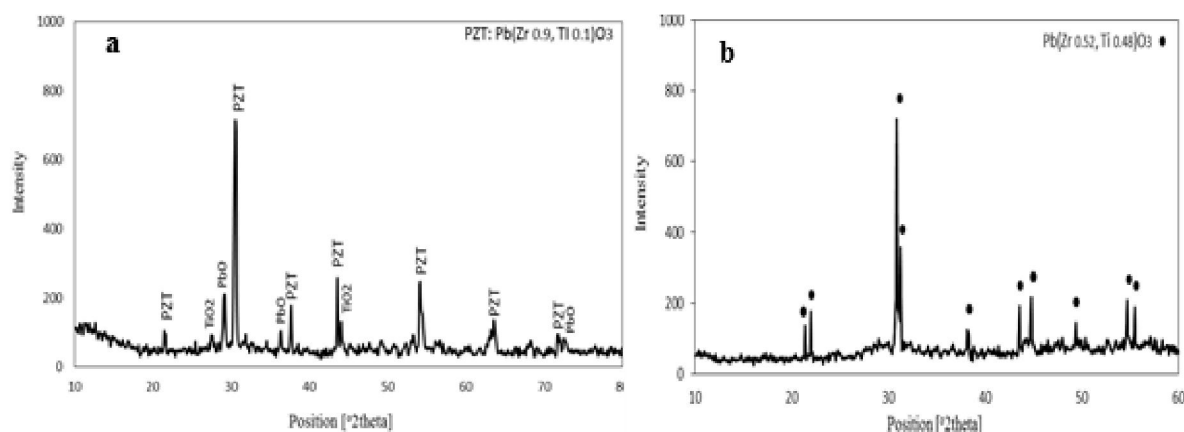
#### 3.1. DTA and TG

According to the DTA analysis results presented in Fig. 1 for mixture powders of PbO, TiO<sub>2</sub> and ZrO<sub>2</sub> ball-milled during 1h, an endothermic reaction has been occurred from 400 to 800 °C that can be related to the formation of PZT. There is an exothermic peak in the temperature of 840 °C corresponding to the crystallization of PZT. Thus, the optimum temperature for the calcination temperature of PZT phase can be 840 - 860 °C. The observation of weight loss from 200 to 400 °C (Fig. 1) can be

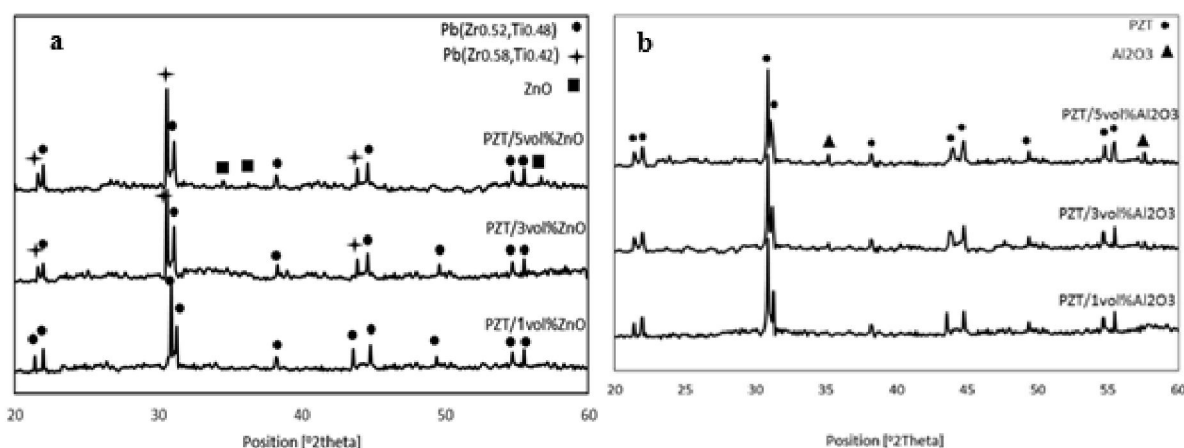
due to removal of the organic compounds and remaining ethanol. Severe weight loss observed at about 900-1000 °C is corresponding to evaporation of PbO. From the DTA results presented in Fig. 1, it is clear that an endothermic peak has been occurred at around 400 °C, which is related to the exit of organic compounds and burning binder in the sample. PZT phase formation has been occurred at a temperature higher than that of 400 °C because of the endothermic nature of influence.

#### 3.2. XRD Results

The XRD results of calcined samples at 850 °C



**Fig. 2.** The XRD patterns taken from the mixture of PZT powders calcined at: (a) 850 °C for 1h; (b) a double-stage of calcination process involving heating at 600 and then 850 °C for 2 hours.



**Fig. 3.** The XRD patterns of: (a) PZT/ZnO; (b) PZT/Al<sub>2</sub>O<sub>3</sub> composites sintered at 1100 °C/2h.

(Fig. 2(a) show that the phases of PbO and TiO<sub>2</sub> are still in the sample and the composition of PZT is Pb(Zr<sub>0.9</sub>Ti<sub>0.1</sub>)O<sub>3</sub>. To achieve the formation of Pb(Zr<sub>0.52</sub>Ti<sub>0.48</sub>)O<sub>3</sub> compound, it has been heat treated under a double stage of calcination process, at first, the powder sample was calcined at 600 °C for 2 hours in order to form PbTiO<sub>3</sub> and PbZrO<sub>3</sub> and then heated at 850 °C for 2h in order to develop of PZT. The XRD results show that the formation of PZT has been completed by applying the double stage of calcination process (Fig. 2(b)).

According to the XRD patterns given in Fig. 3 for PZT/Al<sub>2</sub>O<sub>3</sub> and PZT/ZnO with different percent of ZnO and Al<sub>2</sub>O<sub>3</sub> sintered at 1200 °C for

2h, it has been not occurred any chemical reaction between Al<sub>2</sub>O<sub>3</sub> and or ZnO with PZT matrix during sintering. With increasing amount of ZnO to the PZT, the compound of PZT has been changed from Pb(Zr<sub>0.52</sub>Ti<sub>0.48</sub>)O<sub>3</sub> with tetragonal structure to Pb(Zr<sub>0.58</sub>Ti<sub>0.42</sub>)O<sub>3</sub> with rhombohedra structure which could be due to the proximity of the atomic radius of Zn with Ti and replacing of Ti ions by Zn ones.

### 3.3. Physical and Electrical Properties

According to the results shown in Fig. 4, it is clear that the presence of ZnO or Al<sub>2</sub>O<sub>3</sub> to the



Fig. 4. The effect of ZnO and Al<sub>2</sub>O<sub>3</sub> addition on relative density of PZT/ZnO and PZT/Al<sub>2</sub>O<sub>3</sub> sintered at 1100 °C/2h.



Fig. 5. The effect of ZnO and Al<sub>2</sub>O<sub>3</sub> addition on linear shrinkage of PZT/ZnO and PZT/Al<sub>2</sub>O<sub>3</sub> sintered at 1100 °C/2h.

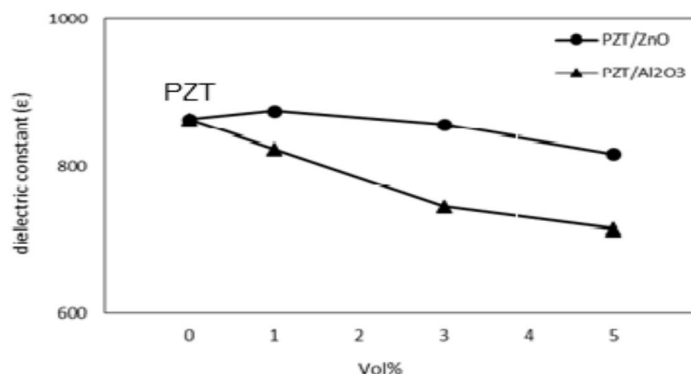
PZT has been associated with the higher relative density of the composite in comparison with that of PZT. The maximum values of the relative density are obtained for the PZT/3%ZnO and PZT/3%Al<sub>2</sub>O<sub>3</sub> composites which are 96.49 and 96.13% respectively. In fact, by presence of the Zn<sup>2+</sup> and Al<sup>3+</sup> ions, the lattice diffusion coefficient is increased by formation of vacancy in PZT and consequently sintering can be more active in the solid state mechanism. On the other hand, the particles of ZnO or Al<sub>2</sub>O<sub>3</sub> which are present between the PZT particles can be associated with a significant prevention of grain growth, and therefore, the grain size is considerably reduced. Moreover, the relative density of the PZT/ZnO composite is more than PZT/Al<sub>2</sub>O<sub>3</sub>, which indicates that ZnO has more effective role than that of Al<sub>2</sub>O<sub>3</sub> in the pure PZT. It is interesting to remark that the melting point of

ZnO is lower than Al<sub>2</sub>O<sub>3</sub> and surface melting of ZnO is greater than Al<sub>2</sub>O<sub>3</sub>.

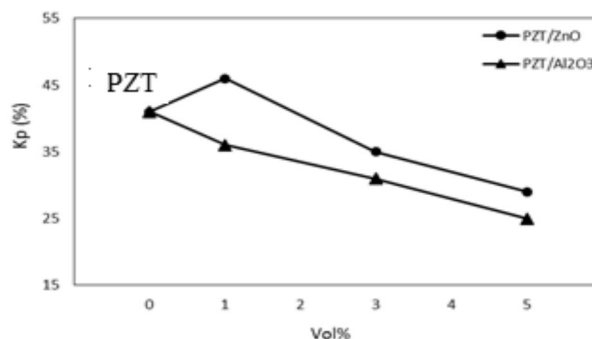
For more information, the linear shrinkage of pure PZT, PZT/ZnO and PZT/Al<sub>2</sub>O<sub>3</sub> composites are shown in Fig. 5. It can be observed that the linear shrinkage has been increased with the amount of ZnO and Al<sub>2</sub>O<sub>3</sub> up to 3Vol%, and then decreases with further increasing of the ZnO and Al<sub>2</sub>O<sub>3</sub> to the PZT.

According to the results presented in Figs. 6 to 9, the addition of Al<sub>2</sub>O<sub>3</sub> and ZnO particles to PZT, the engineering properties such as dielectric constant (Fig. 6), electromechanical factor (Fig. 7) and piezoelectric load factor (Fig. 8) of PZT are reduced while the dielectric loss tangent (Fig. 9) is increased.

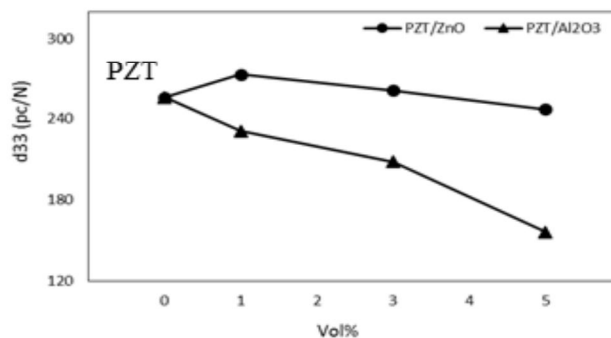
In fact, by presence of ZnO and Al<sub>2</sub>O<sub>3</sub> particles to the pure PZT, the grain size of PZT materials has been decreased and therefore the density of



**Fig. 6.** Diagram of dielectric constant to volume percent (Vol%) of secondary phase for PZT/ZnO and PZT/Al<sub>2</sub>O<sub>3</sub> composites.



**Fig. 7.** Diagram of electromechanical factor to volume percent (Vol%) of secondary phase for PZT/ZnO and PZT/Al<sub>2</sub>O<sub>3</sub> composites.



**Fig. 8.** Diagram of piezoelectric load factor to volume percent (Vol%) of secondary phase for PZT/ZnO and PZT/Al<sub>2</sub>O<sub>3</sub> composites.

grain boundary can be increased causing a significant scattering and reduction of electrical properties. On the other hand, Zr<sup>4+</sup> and Ti<sup>4+</sup> ions in perovskite lattice can be replaced by Zn<sup>2+</sup> and Al<sup>3+</sup> ones which can be resulted to the significant reduction of distance between the centers of positive and negative dipoles and consequently

decreasing of piezoelectric properties. Moreover, the dielectric constant, electromechanical factor and piezoelectric load factor are increased slightly for PZT/1vol% ZnO composite. This enhancement can be firstly due to the increasing of relative density and reduction of porosity, and secondly proximity of ionic radio of Zn<sup>2+</sup> with

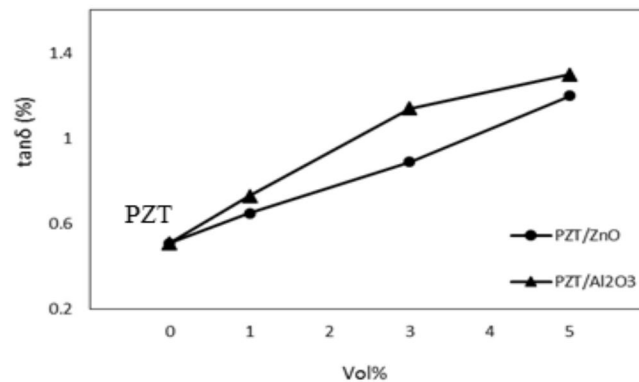


Fig. 9. Diagram of dielectric loss tangent to volume percent (Vol%) of secondary phase for PZT/ZnO and PZT/Al<sub>2</sub>O<sub>3</sub> composites.

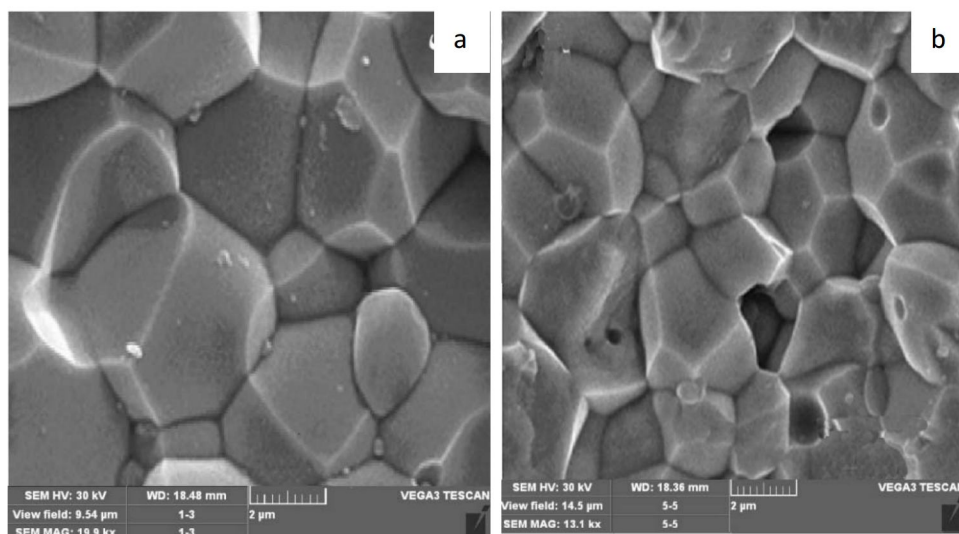
Ti<sup>4+</sup> and Zr<sup>4+</sup>. Replacing of Zr<sup>4+</sup> or Ti<sup>4+</sup> by Zn<sup>2+</sup> has caused a significant level of vacancy in crystalline lattice and therefore increasing of space between center of position and negative dipoles.

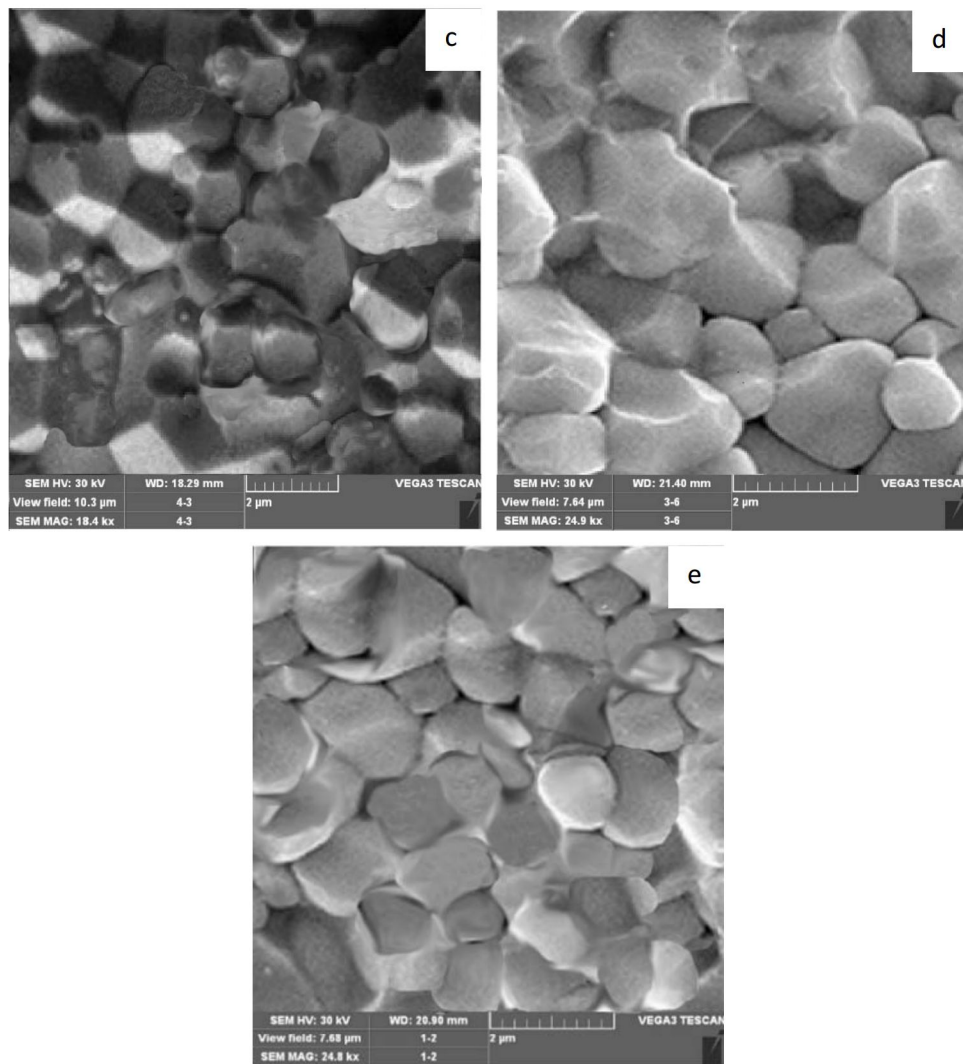
### 3. 4. Microstructural Features and Mechanical Properties

According to SEM micrographs of PZT, PZT/ZnO and PZT/Al<sub>2</sub>O<sub>3</sub> samples shown in Fig. 10, the presence of ZnO and Al<sub>2</sub>O<sub>3</sub> in PZT as a second phase has resulted to a finer grain microstructure. In fact, the particles of ZnO or Al<sub>2</sub>O<sub>3</sub> in grain boundaries of PZT are associated with lowering grain growth during sintering process and so the strength of obtained

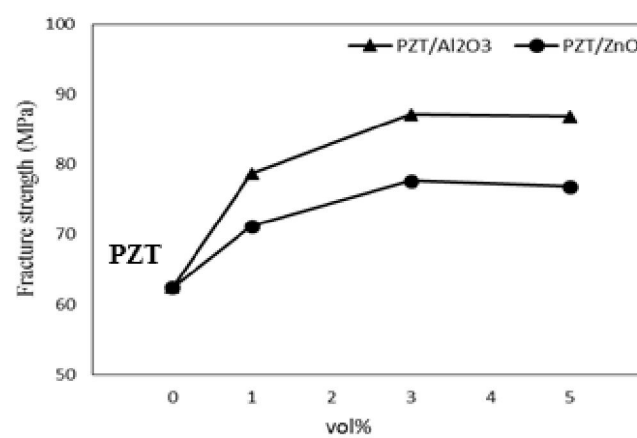
composites can be higher than that of PZT ceramic (Fig. 11). On the other hand, these particles prevent the formation and propagation of crack in grain boundary areas.

Because of higher hardness and elastic modulus of Al<sub>2</sub>O<sub>3</sub> (12 GPa and 375 GPa, respectively) compared to that of ZnO (5 GPa and 210 GPa, respectively), the increasing of strength for PZT/Al<sub>2</sub>O<sub>3</sub> composite is more than PZT/ZnO. According to Fig. 12, the hardness for both types of composites are higher than that of PZT monolithic ceramic that can be due to a finer microstructure and higher relative density developed in the composite samples. The higher hardness for PZT/Al<sub>2</sub>O<sub>3</sub> composite can be related to the higher hardness of Al<sub>2</sub>O<sub>3</sub> particles in comparison with the lower hardness of ZnO. The

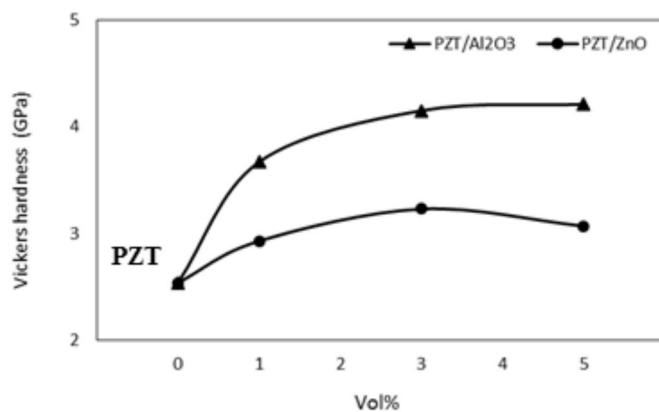




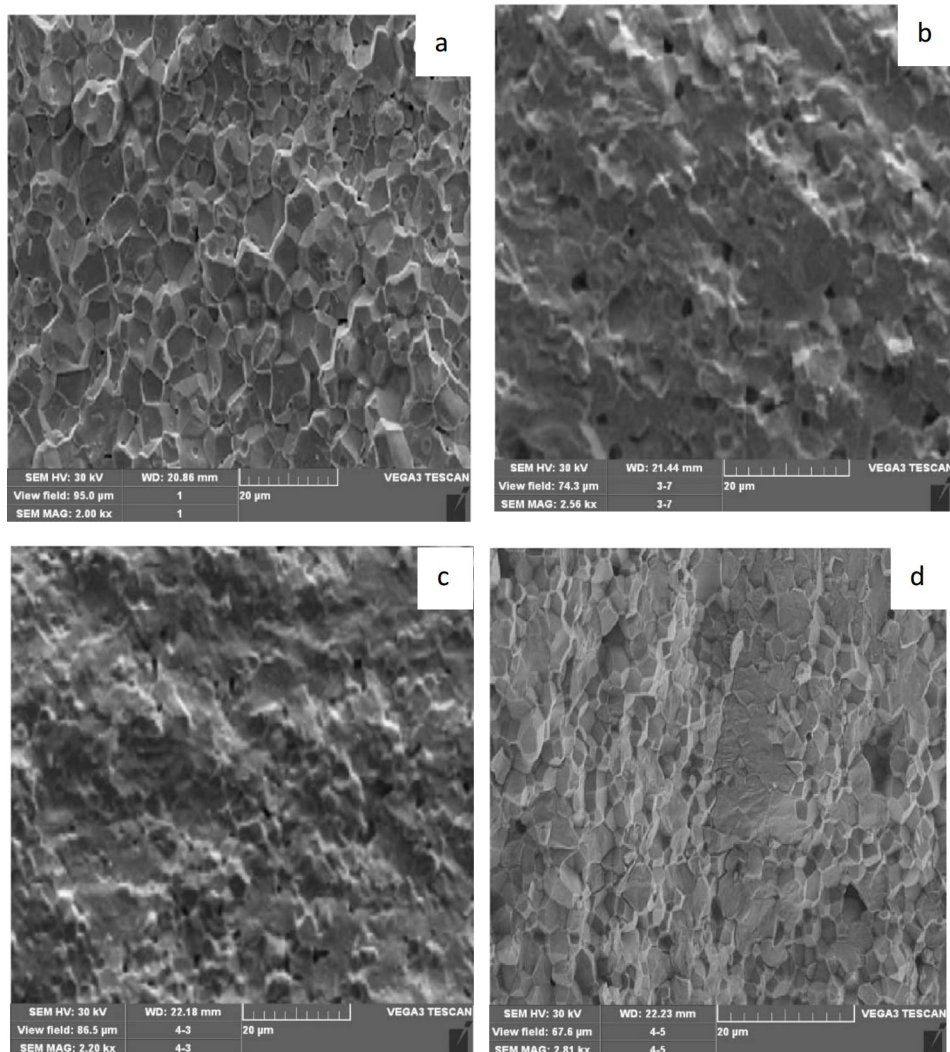
**Fig. 10.** SEM images of: a) PZT; b) PZT/1Vol%ZnO; c) PZT/3Vol%ZnO; d) PZT/1Vol%Al<sub>2</sub>O<sub>3</sub>; and e) PZT/3Vol%Al<sub>2</sub>O<sub>3</sub>.

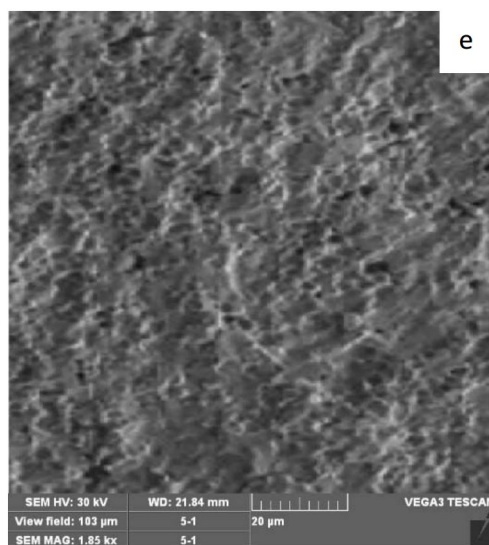


**Fig. 11.** Bending strength as a function of volume percent (Vol%) of secondary phase for pure PZT, PZT/Al<sub>2</sub>O<sub>3</sub> and PZT/ZnO composites.

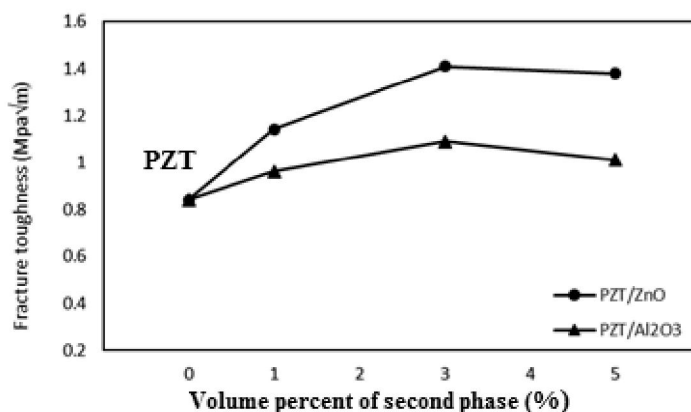


**Fig. 12.** Vickers hardness as a function of volume percent (Vol%) of secondary phase for pure PZT; PZT/Al<sub>2</sub>O<sub>3</sub> and PZT/ZnO composites.





**Fig. 13.** SEM images of fracture surfaces: a) PZT; b) PZT/1Vol%ZnO; c) PZT/3Vol%ZnO; d) PZT/1Vol%Al<sub>2</sub>O<sub>3</sub>; and e) PZT/3Vol%Al<sub>2</sub>O<sub>3</sub>.



**Fig. 14.** Fracture toughness as a function of volume percent (Vol%) of secondary phase for PZT/ZnO and PZT/Al<sub>2</sub>O<sub>3</sub> composites.

most hardening increasing have been occurred for PZT/5Vol%Al<sub>2</sub>O<sub>3</sub> and PZT/3Vol%ZnO composite samples which have been associated with the higher hardness of 66% and 27%, respectively in comparison with that of PZT hardness value.

According to the SEM micrographs of fracture surfaces of PZT, PZT/ZnO and PZT/Al<sub>2</sub>O<sub>3</sub> samples shown in Fig. 13, the dominate mechanism of fracture for PZT sample is intergranular. However, the fracture surfaces of the PZT/ZnO and PZT/Al<sub>2</sub>O<sub>3</sub> composite samples are rougher than that of the monolithic ones and that the roughness of fracture surfaces has been

increased with increasing of ZnO and Al<sub>2</sub>O<sub>3</sub> content. In other words, the fracture behavior of PZT/ZnO and PZT/Al<sub>2</sub>O<sub>3</sub> composites is a mixture of transgranular and intergranular modes.

In fact, by presence of ZnO or Al<sub>2</sub>O<sub>3</sub> particles in the pure PZT, the strength of grain boundaries has been improved and consequently the percentage of intragranular fracture is not predominate, although the strength and toughness can be simultaneously increased (Figs 11, 14).

According to the light micrographs of Vickers indentation presented in Fig.15, the crack length created on the composite sample surfaces is much

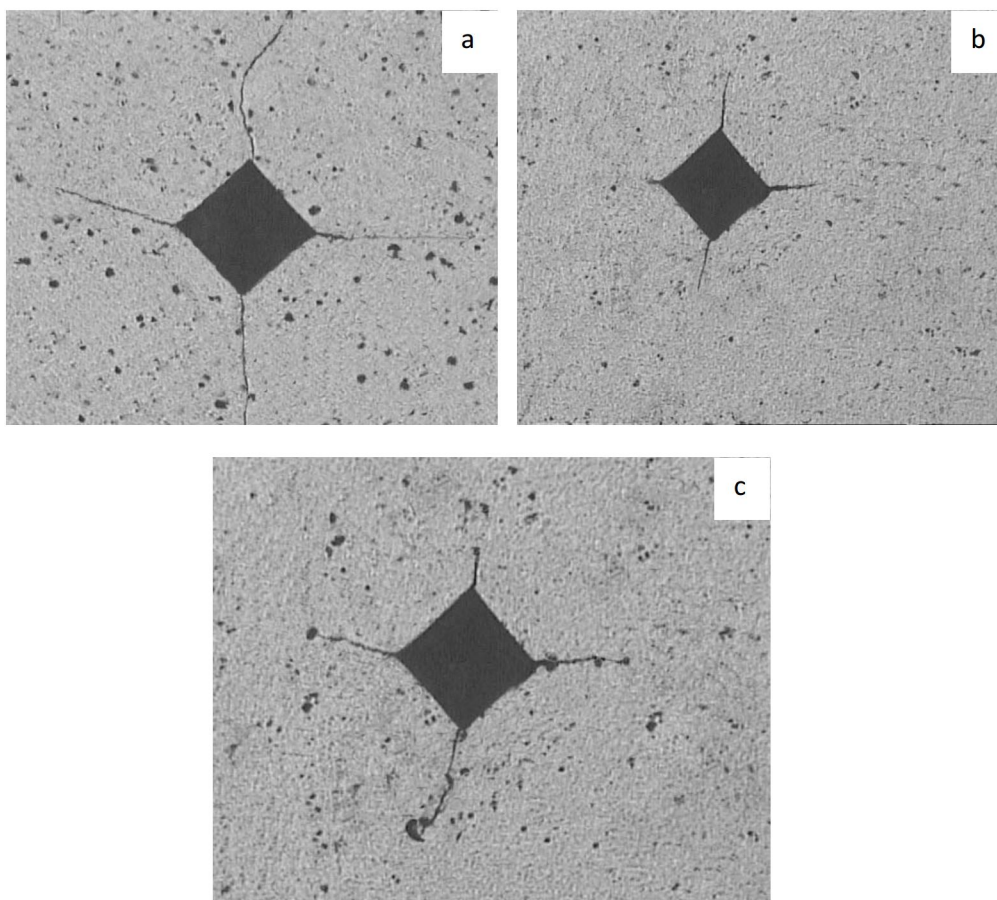


Fig. 15. Optical microscope images of Vickers indentation: a) PZT; b) PZT/3Vol%Al<sub>2</sub>O<sub>3</sub>; and c) PZT/3Vol%ZnO

less than that of PZT samples indicating a higher resistance to crack growth has been occurred for the composite samples. Moreover, a higher relative density, the higher strength and more resistance to the propagation of crack in grain boundary are associated for the higher toughness of the composite samples. The higher resistance to crack growth in composite samples can be related to the crack bridging developed by Al<sub>2</sub>O<sub>3</sub> and ZnO particles, which reduces the energy of crack growth. Moreover, the higher toughness of PZT/ZnO composite samples in comparison with that of PZT/Al<sub>2</sub>O<sub>3</sub> samples can be due to the higher density of PZT/ZnO as well.

#### 4. CONCLUSIONS

1. A double stage of calcination involving firstly heated at 600°C and then at 800 °C

for 2 hours has been related with a perfect formation of PZT.

2. Al<sub>2</sub>O<sub>3</sub> and ZnO particles as a reinforced phase are non-sensitive to chemical reaction with PZT and are compatible with it.
3. By adding of Al<sub>2</sub>O<sub>3</sub> and ZnO particles to the PZT ceramic, the sinterability has been increased and the highest relative density is obtained for PZT/3Vol%ZnO and PZT/3Vol%Al<sub>2</sub>O<sub>3</sub> samples.
4. By adding of Al<sub>2</sub>O<sub>3</sub> and ZnO particles simultaneously to the PZT samples, a finer microstructure has been obtained in comparison to that of pure PZT and PZT based composite samples (Al<sub>2</sub>O<sub>3</sub>/PZT and ZnO/PZT).
5. Fracture mechanism of PZT samples is intergranular mode while for PZT/ZnO and

- PZT/Al<sub>2</sub>O<sub>3</sub> composites are a combination of intergranular and intragranular modes.
6. By adding of Al<sub>2</sub>O<sub>3</sub> and ZnO to the PZT samples, the strength, fracture toughness and hardness are increased. The highest strength and hardness values are obtained for PZT/Al<sub>2</sub>O<sub>3</sub> samples in the manner of 85MPa and 4.5 GPa, respectively; while the highest toughness is obtained for PZT/ZnO composite ones (1.4 MPa.m<sup>1/2</sup>).
  7. By adding of Al<sub>2</sub>O<sub>3</sub> and ZnO to the PZT samples, the electrical properties such as dielectric constant, piezoelectric load factor and electromechanical factor are slightly reduced while the loss tangent is increased.

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